# H<sub>3</sub> + in dense and diffuse clouds

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Interstellar  ${\rm H_3}^+$  has been detected in dense as well as diffuse clouds using three 3.7 µm infrared spectral lines of the  $v_2$  fundamental band. Column densities of  ${\rm H_3}^+$  from  $(1.7–5.5)\times 10^{14}~{\rm cm}^{-2}$  have been measured in dense clouds in absorption against the infrared continua of the deeply embedded young stellar objects GL2136, W33A, MonR2 IRS 3, GL961E, and GL2591. Strong and broad  ${\rm H_3}^+$  absorptions have been detected in dense and diffuse clouds towards GC IRS 3 and GCS3-2 in the region of the galactic center. A large column density of  ${\rm H_3}^+$ , comparable to that of a dense cloud, has been detected towards the visible star Cygnus OB2 No. 12, which has a line of sight that crosses mostly diffuse clouds. The  ${\rm H_3}^+$  chemistry of dense and diffuse clouds are discussed using a very simple model. Some future projects and problems are discussed.

#### 1 Background

Protonated hydrogen, H<sub>3</sub><sup>+</sup>, is the simplest stable polyatomic molecule, and was discovered in 1911 by J. J. Thompson.<sup>1</sup> It is the most abundant ion in hydrogen plasmas, as initially discovered by A. J. Dempster.<sup>2</sup> In 1925, Hogness and Lunn<sup>3</sup> introduced the celebrated ion–neutral reaction

$$H_2^+ + H_2 \rightarrow H_3^+ + H$$
 (I)

as the primary mechanism for  $\rm H_3^+$  production. By the 1930s, the predominance of  $\rm H_3^+$  among cations in hydrogen plasmas was well established experimentally,<sup>4</sup> and the systematic theoretical studies by Eyring, Hirschfelder and others had explained the large cross-section<sup>5</sup> and high exothermicity<sup>6</sup> of reaction (I). Readers are referred to a review<sup>7</sup> for more details of early works.

### 1.1 Interstellar H<sub>3</sub><sup>+</sup>

The 1961 paper by Martin *et al.*<sup>8</sup> seems to be the first to suggest that  $H_3^+$  should be abundant in interstellar space. In 1970, Stecher and Williams discussed the production and destruction rates of interstellar  $H_3^+$ . The first numerical estimate of the interstellar  $H_3^+$  concentration was reported by Solomon and Werner, who also took the decisive step of introducing the cosmic ray as the major agent of ionization. Their estimate of the  $H_3^+$  fraction  $X(H_3^+) \equiv [H_3^+]/[\Sigma H] \approx 10^{-6}$  (where  $[\Sigma H]$  denotes the total number density of hydrogen atoms), can be contrasted to the value  $10^{-8}$  derived in this paper. de

Jong<sup>11</sup> did similar calculations and obtained  $X({\rm H_3}^+) \approx 0.4-1.0 \times 10^{-6}$ . Reaction (I) was also used by Glassgold and Langer<sup>12</sup> as the mechanism for cosmic ray heating of molecular clouds and by Watson<sup>13</sup> in his theory of isotope fractionation in interstellar HD.

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In 1973, the science of interstellar H<sub>3</sub><sup>+</sup> acquired a new dimension, when Watson<sup>14</sup> and Herbst and Klemperer<sup>15</sup> independently proposed a network of ion–neutral reactions as the mechanism to generate the wide variety of simple molecules that had been observed in interstellar space by radioastronomers.<sup>16</sup> This idea, which was perhaps influenced by the millimeter wave detection of X-ogen by Buhl and Snyder<sup>17</sup> and its subsequent identification as HCO<sup>+</sup> by Klemperer,<sup>18</sup> revealed that H<sub>3</sub><sup>+</sup> plays a central role in interstellar chemistry. Because of the relatively low proton affinity of H<sub>2</sub> (4.5 eV), H<sub>3</sub><sup>+</sup> protonates practically all atoms and molecules through the general reaction

$$H_3^+ + X \to HX^+ + H_2$$
 (II)

(He, Ne, Ar, N and O<sub>2</sub> are notable exceptions). After protonation, the HX<sup>+</sup> combines with other species through the reaction

$$HX^+ + Y \to XY^+ + H \tag{III}$$

and initiates a network of chemical reactions. The detailed numerical model calculation of such networks in the classic paper by Herbst and Klemperer<sup>15</sup> explained many of the observed results. Their success triggered an avalanche of papers and reviews on interstellar chemistry based on the ion–neutral reaction scheme. While they are too numerous to cite, many important papers can be traced from the references given in three works that were essential in the preparation of this discussion: the paper by de Jong  $et\ al.^{19}$  on  $H_3^+$  chemistry, the chemical model calculation for diffuse clouds by van Dishoeck and Black,<sup>20</sup> and the model for dense clouds by Lee  $et\ al.^{21}$ 

#### 1.2 The search for $H_3$ <sup>+</sup>

'It is likely that  $H_3^+$  is present in the interstellar medium, since  $H_2^+$  ions must be formed from the  $H_2$  molecules present in the interstellar medium either by light absorption beyond 805 Å or by cosmic rays and since each  $H_2^+$  ion will, upon collision with a neutral  $H_2$  molecule, immediately form  $H_3^+$  according to reaction (I). However, the possibility of detecting  $H_3^+$  in interstellar space depends on the discovery of a spectrum of this molecule in the laboratory.'

Gerhard Herzberg, 1967<sup>22</sup>

Herzberg thus attempted together with J. W. C. Johns to observe the infrared  $v_2$  fundamental band of  $H_3^+$  in emission. Since  $H_3^+$  does not have well-bound electronic excited states,<sup>7</sup> no ultraviolet or visible spectrum is expected. Its symmetric equilateral triangle structure also forbids a conventional rotational spectrum. Therefore, the infrared active degenerate  $v_2$  band is the most straightforward way to detect interstellar  $H_3^+$ .

There were other proposals based on radioastronomy, which is by far the most sensitive method of detecting interstellar molecules. Salpeter and Malone<sup>23</sup> pointed out the possibility of detecting H<sub>3</sub><sup>+</sup> using its radio recombination lines, which are slightly shifted from the H<sup>+</sup> recombination lines due to the difference in reduced mass. The recombination lines of He<sup>+</sup> and C<sup>+</sup> were well known. An emission line feature was noted between the 85αH<sup>+</sup> and 85αHe<sup>+</sup> in NGC2024<sup>24</sup> but its frequency was not quite right.<sup>25</sup> The detection of H<sub>3</sub><sup>+</sup> using this technique is probably very difficult because of the low abundance of H<sub>3</sub><sup>+</sup> in H II regions, where recombination lines are strong.

Another proposal<sup>26</sup> was to detect the deuterated species H<sub>2</sub>D<sup>+</sup>. The deuteration shift of the center of charge produces an effective dipole

Another proposal<sup>26</sup> was to detect the deuterated species  $H_2D^+$ . The deuteration shift of the center of gravity from the center of charge produces an effective dipole moment of 0.6 D and makes the rotational spectrum active in the radio and far-infrared region. The abundance of  $H_2D^+$  is much higher than expected from the natural abun-

dance of deuterium because of the efficient isotope fractionation, first explained by Watson.  $^{13,\ 27}$  A detection of  $H_2D^+$  emission at 372 GHz was reported  $^{28}$  in NGC2264 but was later negated.  $^{29}$  A more recent detection of an  $H_2D^+$  signal by Boreiko and Betz  $^{30}$  in absorption at 1370 GHz in IRc2 has a better signal-to-noise ratio, though its authenticity has yet to be confirmed. The search for interstellar  $H_3^+$  using its centrifugal distortion spectrum  $^{31}$  was noted  $^{32}$  and advocated by Draine and Woods  $^{33}$  for studies of high temperature objects such as the X-ray heated clouds NGC6240.

The most straightforward way of searching for  ${\rm H_3}^+$  became possible in 1980 when its infrared  $v_2$  band spectrum was discovered in the laboratory.<sup>34</sup> An immediate attempt to detect  ${\rm H_3}^+$  in the Becklin–Neugebauer (BN) source in Orion using the FTIR spectrometer at the 4 m Mayall Telescope of the Kitt Peak National Observatory (KPNO) was unsuccessful.<sup>35</sup> A search by two of the authors (T.R.G. and T.O.) was continued using a Fabry–Perot interferometer and a generation of cooled grating spectrometers (CGS) at the UK Infrared Telescope (UKIRT) on Mauna Kea, during which negative results for several sources were published.<sup>36</sup> The search was also attempted by many other groups and some of them published their inconclusive results.<sup>37–40</sup>

From 1988 to 1994, our observational work was diverted to studying  ${\rm H_3}^+$  in planetary ionospheres following the discovery of strong  ${\rm H_3}^+$  emission in the auroral regions of Jupiter, Saturn and Uranus,<sup>41</sup> as well as the Comet SL-9 impact on Jupiter. During this time the resolution, sensitivity and reliability of observational infrared spectrometers improved dramatically—a major factor in this development was the use of infrared detector arrays. In 1994, an infrared absorption line of  ${\rm H_2}$  in NGC2024 was detected at the NASA Infrared Telescope Facility (IRTF).<sup>42</sup> This detection suggested that the sensitivity of IRTF's CSHELL spectrometer had reached the point necessary for  ${\rm H_3}^+$  detection, since it was known<sup>35</sup> that the ratio of the intensities of the  ${\rm H_3}^+$  dipole transition and the  ${\rm H_2}$  quadrupole transition ( $\approx 10^9$ ) just about cancelled the abundance ratio of  ${\rm H_3}^+$  to  ${\rm H_2}$  ( $\approx 10^{-9}$ ). Our applications for observing time using CSHELL on IRTF were rejected for three consecutive terms, and interstellar  ${\rm H_3}^+$  was instead detected by the CGS4 spectrometer at UKIRT, in 1996. Since then our observations have progressed, yielding positive detections in dense clouds, diffuse clouds, and in the region of the galactic center.

# 2 The $H_3$ + spectrum

Since the details of the  $v_2$  fundamental band vibration-rotation spectrum were given in a recent Faraday Discussion,<sup>43</sup> here we simply note two characteristics of the  $H_3$ <sup>+</sup> spectrum: the vibrational frequency and the rotational level structure. Both of these characteristics have important consequences for the observation of interstellar  $H_3$ <sup>+</sup>.

#### 2.1 Vibrational frequency

When a proton is added to an  $H_2$  molecule, the extra charge pushes the two protons away and the equilibrium interproton distance increases from 0.74 Å to 0.87 Å. The vibrational frequency is reduced from 4161.2 cm<sup>-1</sup> to  $v_1 = 3178.3$  cm<sup>-1</sup> <sup>44</sup> and  $v_2 = 2521.3$  cm<sup>-1</sup>.<sup>45</sup> The infrared active  $v_2$  band is located in a region free from spectral lines of ordinary molecules made from atoms with high cosmic abundance. The hydrogen stretching vibrations of C—H, N—H and O—H bonds are all much higher in frequency and even the high J P-branch lines of light molecules, such as  $CH_4$ ,  $NH_3$  and  $H_2O$ , do not reach the 4  $\mu$ m region. The hydrogen bending vibrations are all too low in frequency and their R-branches do not reach this region. The stretching vibrations of heavier elements such as C=O, C=N and C=C are the closest to this region, but their rotational structures do not extend much in frequency because of their larger moments of inertia. Fig. 1, which was adapted from Genzel's review, 46,47 shows the unique position

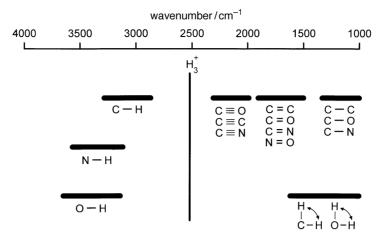


Fig. 1 Position of the  $v_2$  band of  $H_3^+$  compared with other common molecular vibrations. Note that  $H_3^+$  is relatively free of interference from spectral lines of ordinary molecules made from atoms with high cosmic abundance. This figure is adapted from Genzel's review.<sup>46,47</sup>

of the  ${\rm H_3}^+ \nu_2$  band. This freedom from the spectra of other molecules is the reason for the extremely pure  ${\rm H_3}^+$  emission spectrum of Jupiter reported by Maillard *et al.*<sup>48</sup> More importantly for observations of interstellar  ${\rm H_3}^+$ , this favored location of the band origin makes our ground-based observation relatively unhindered by interference with molecules in the terrestrial atmosphere (L window). The only spectral lines that interfere with our observations are deuterium stretching vibrations, notably of HDO, and overtone and combination bands, notably of the  $\nu_2 + \nu_4$  band of  ${\rm CH_4}$ , which are of course orders of magnitude weaker than the fundamental bands. Had the  $\nu_2$  band appeared in the 3  $\mu$ m region, it would have been next to impossible to detect interstellar  ${\rm H_3}^+$  from ground-based observatories.

#### 2.2 Rotational level structure

Because of its small mass,  $\mathrm{H_3}^+$  has large rotational constants<sup>45</sup>  $B=43.56~\mathrm{cm}^{-1}$  and  $C=20.61~\mathrm{cm}^{-1}$ , and only the lowest few levels are significantly populated in molecular clouds with temperatures of  $10-100~\mathrm{K}$ . The structure of the lowest rotational levels is shown in Fig. 2, where the energy scale is expressed in temperature (Kelvin). J is the rotational angular momentum quantum number and K is its projection onto the  $C_3$  symmetry axis. A special characteristic of this rotational structure is that the lowest level with J=K=0 (shown in Fig. 2 with a broken line) is not allowed by the Pauli exclusion principle. According to Dirac's statement of the Pauli principle,<sup>49,50</sup> the total wavefunction must change sign when two protons are interchanged but must remain invariant when the three protons are cyclicly permuted. The wavefunction of the lowest rotational level is simply a constant and these conditions cannot be simultaneously satisfied, whether this rotational wavefunction is combined with the *ortho* nuclear spin function (in which all proton spins are parallel,  $I=\frac{3}{2}$ , and the first condition is not satisfied) or with the *para* nuclear spin function (in which one proton spin is antiparallel,  $I=\frac{1}{2}$ , and the second condition is not satisfied).

This leaves the J=1, K=1 level of para- $\dot{H}_3^+$  as the lowest ground rotational level. This and the next lowest level with J=1, K=0 of ortho- $H_3^+$ , which is higher than the ground level by 32.9 K, are the only levels that are significantly populated for temperatures of 5–50 K. These two levels contain nearly equal populations of molecules,

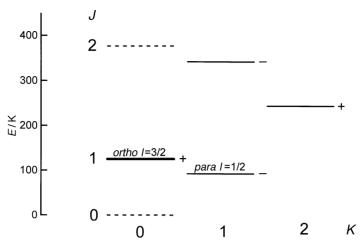


Fig. 2 Structure of the lowest rotational levels of  $H_3^+$ . Broken lines represent forbidden levels, the bold line indicates a level with the *ortho*  $(I=\frac{3}{2})$  spin modification, the thin lines indicate levels with the *para*  $(I=\frac{1}{2})$  spin modifications. The (+) and (-) signs indicate the parity of the levels. The transitions studied in interstellar space arise from the J=1 levels.

since the higher spin statistical weight of ortho- $H_3^+$  ( $g_I = 2I + 1 = 4$ ) than that of para- $H_3^+$  ( $g_I = 2$ ) is approximately compensated for by the Boltzmann factor  $\exp{(-32.9/T)}$ . We thus have six spectral lines of comparable intensities at 30 K as shown in Fig. 3, two from ortho- $H_3^+$  [R(1,0) and Q(1,0)] and four from para- $H_3^+$  [R(1,1)<sup>+</sup>, R(1,1)<sup>-</sup>, Q(1,1) and P(1,1)]. The existence of six lines makes the observation flexible—we may choose lines that are freest from the telluric interference depending on the weather and the Doppler shift of the night. Two of the spectral lines, R(1,1)<sup>+</sup> of para- $H_3^+$  and R(1,0) of

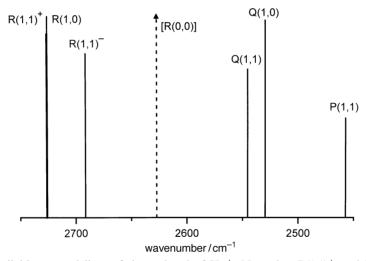


Fig. 3 Six available spectral lines of the  $v_2$  band of  $H_3^+$ . Note that  $R(1,1)^+$  and R(1,0) form a doublet with spacing of 0.321 cm<sup>-1</sup>, which is particularly useful for astronomical observations. The broken line marks the hypothetical position of the transition arising from the forbidden level J = K = 0. This line would have an intensity four times that of the other strongest lines if it were allowed. These intensities are calculated for an assumed temperature of 30 K.

ortho-H<sub>3</sub><sup>+</sup>, are separated by only 0.321 cm<sup>-1</sup> and are particularly useful for the measurement of temperature and for confirmation of detections.

Had the lowest J = K = 0 level been allowed, the spectrum of  $H_3^+$  would be like an atomic spectrum, since most of the molecules would be in the lowest level, and the R(0,0) line would be the only strong line, at the position shown with a broken arrow in Fig. 3.

#### 3 Observed results

Observations of interstellar  ${\rm H_3}^+$  have so far been conducted using three infrared spectrometers: the CGS4 at UKIRT with spectral resolution  $R\approx 20\,000$ , the Phoenix spectrometer at KPNO with  $R\approx 60\,000$ , and the CSHELL at NASA IRTF with  $R\approx 20\,000$ . All of them have produced positive results. Interstellar  ${\rm H_3}^+$  has been found in gravitationally bound dense clouds with high density ( $[\Sigma {\rm H}] \approx 10^3-10^5~{\rm cm}^{-3}$ ) as well as in unbound diffuse clouds with low density ( $10-10^3~{\rm cm}^{-3}$ ).

#### 3.1 H<sub>3</sub> + in dense clouds

The first spectra of interstellar  ${\rm H_3}^+$  were detected towards the young stellar objects (YSOs) GL2136 and W33A, which are deeply embedded in dense molecular clouds. These spectra were obtained with CGS4 at UKIRT on the nights of April 25, June 10 and July 15, 1996. These YSOs were chosen because of their infrared brightness and because of their large column densities of foreground gas. In addition, it was thought advantageous to use carbon depleted clouds where  ${\rm H_3}^+$  is destroyed less by the proton hop reaction (II). Strong absorptions of solid CO frozen on dust grains have been reported 33,54 although the depletions might not be large.

The  $R(1,0)-R(1,1)^+$  doublet of  $H_3^+$  mentioned earlier was used for the detection. The observed signal to noise ratios of the absorption lines were by no means great, but the Doppler shift of the doublet lines due to the earth's orbital motion from April 25 to July 15 convinced us that the signals were genuine (see Fig. 4).

Subsequent observations revealed interstellar H<sub>3</sub><sup>+</sup> in dense clouds towards three other YSOs: MonR2 IRS 3 and GL961E (February 11–14, 1997, at UKIRT), and

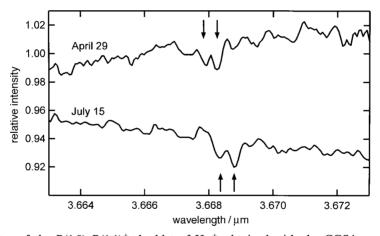


Fig. 4 Spectra of the R(1,0)-R(1,1)<sup>+</sup> doublet of H<sub>3</sub><sup>+</sup> obtained with the CGS4 spectrometer at UKIRT along the line of sight to GL2136. The upper trace was obtained on 29 April, 1996, while the lower trace was obtained on 15 July, 1996. The observed Doppler shift of the doublet (marked with arrows) between the two dates matches that expected from the Earth's orbital motion, providing convincing evidence that the doublet is genuine.

GL2591 (July 11–12, 1997, at UKIRT). The observed equivalent widths  $W_{\nu}$  yield the  $H_3^+$  column densities using the standard formula

$$W_{\nu} \equiv \int \left[ \Delta I(\nu) / I(\nu) \right] d\nu = (8\pi^3 \nu / 3hc) N |\mu|^2$$
 (1)

where  $|\mu|^2$  is the square of the transition dipole moment. The spectral lines of *ortho*- $H_3^+$  and *para*- $H_3^+$  give their column densities  $N_o$  and  $N_p$  separately, and their sum gives the total  $H_3^+$  column density  $N(H_3^+)$ . The ratio of  $N_o$  and  $N_p$  gives the temperature of the clouds using the standard formula

$$\frac{N_o}{N_p} = \frac{g_o}{g_p} e^{(-\Delta E/kT)} = 2 e^{(-32.9/T)}$$
 (2)

These results are summarized in Table 1. We have also studied the infrared sources GL490, GL989, LkH $\alpha$  101, MonR2 IRS 2, M17 IRS 1, S140 IRS 1, W3 IRS 5, Elias 29, NGC2024 IRS 2 and BN. So far, our data reduction has not provided evidence of column densities at the level of ca.  $2-3 \times 10^{14}$  cm $^{-2}$ , but careful reprocessing of these spectra continues. The lack of strong  $H_3^+$  absorption towards NGC2024 IRS 2 and BN was particularly surprising in view of the large column density of  $H_2$  reported in the former<sup>42</sup> and the observed richness of molecules in the latter. We believe that these non-detections are not due to the absence of  $H_3^+$  in the clouds but are simply due to the short column length of the clouds in front of the source (see the discussion in Section 4.1). More details of our study of dense clouds will be published elsewhere.<sup>56</sup>

## 3.2 H<sub>3</sub> + in diffuse clouds

During our survey of  ${\rm H_3}^+$  in dense clouds, we observed strong and broad  ${\rm H_3}^+$  absorption signals in the direction of the infrared sources GC IRS 3 and GCS3-2 (July 11–12, UKIRT), in the region near the galactic center. These sources are thought to be 8 kpc away and their lines of sight may cross several clouds, both dense and diffuse. Indeed McFadzean *et al.*<sup>57</sup> reported observational evidence for two components in the extinction: the 3.0  $\mu$ m ice absorption (a signature of dense clouds) and the 3.4  $\mu$ m hydrocarbon absorption (a signature of diffuse clouds). More details of our galactic center observations will be published separately.<sup>58</sup>

The galactic center results led us to try Cygnus OB2 No. 12, a visible star with high extinction discovered in 1954.<sup>59</sup> It is generally believed that this star is obscured largely by diffuse, low density clouds containing little molecular material.<sup>60</sup> We clearly observed

			1	
	position			
infrared source	α (1950)	δ (1950)	$N({\rm H_3}^+)/(10^{14}~{\rm cm}^{-2})^a$	T/K
dense clouds				
GL2136	18:19:36.6	-13:31:40	$3.6 \pm 0.6$	$35 \pm 4$
W33A	18:11:44.2	-17:52:56	$5.5 \pm 1.9$	$30 \pm 6$
MonR2 IRS 3	06:05:21.8	-06:22:26	$2.1 \pm 0.7$	$24 \pm 4$
GL961E	06:31:59.1	+04:15:10	$1.7 \pm 0.7$	$24 \pm 5$
GL2591	20:27:35.8	+40:01:14	$2.0 \pm 1.0^{b}$	
diffuse clouds				
Cyg OB2 No. 12	20:30:53.4	+ 41 : 03 : 52	$3.8 \pm 0.5$	$20 \pm 4$

**Table 1** Positions and derived column densities and temperatures for H<sub>3</sub><sup>+</sup> sources

<sup>&</sup>lt;sup>a</sup> Statistical uncertainties ( $3\sigma$ ) are quoted in parentheses but systematic errors are difficult to estimate and might be larger. <sup>b</sup> Estimated systematic uncertainty is given for GL2591, as this spectrum is not yet fully reduced.

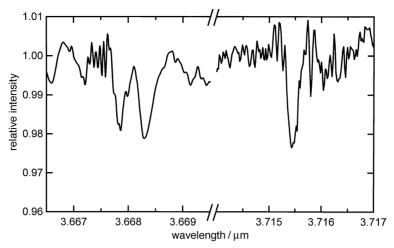


Fig. 5 Spectra of the line of sight towards the visible star Cygnus OB2 No. 12. The left trace, showing the R(1,0)-R(1,1)<sup>+</sup> doublet of H<sub>3</sub><sup>+</sup>, was obtained with CGS4 at UKIRT on 11 July, 1997. The right trace, showing the R(1,1)<sup>-</sup> line of H<sub>3</sub><sup>+</sup>, was obtained with the new Phoenix spectrometer at KPNO on 17 September, 1997. The high frequency interference in the CGS4 spectrum near 3.6675 μm is due to the removal of a telluric CH<sub>4</sub> absorption line.

the  $H_3^+$  R(1,0)-R,(1,1)<sup>+</sup> doublet (July 11-12, UKIRT) and the R(1,1)<sup>-</sup> singlet (September 15-17, KPNO).<sup>61</sup> Because of the high humidity in Arizona in September, strong and wide telluric HDO lines ( $v_2$  band  $1_{10} \leftarrow 1_{11}$  and  $4_{22} \leftarrow 4_{23}$ ) made the observation of the doublet impossible, but the singlet (which has only CH<sub>4</sub> lines nearby) was clearly observed. The observed spectrum is shown in Fig. 5. Using the observed equivalent widths of the lines and eqn. (1), we obtain the remarkable result that the column density of  $H_3^+$  in the direction of Cygnus OB2 No. 12 is  $(3.8 \pm 0.5) \times 10^{14}$  cm<sup>-2</sup>, comparable to that of the dense clouds listed in Table 1. van Dishoeck and Black<sup>20,62</sup> reported their extensive chemical model calculation in diffuse clouds and predicted high column densities of  $H_3^+$ , but their calculation was based on an extremely small electron recombination rate constant, which has since been demonstrated to be too low by more than three orders of magnitude.<sup>63</sup> Calculations given in the next section show that the large column density of  $H_3^+$  in the diffuse clouds towards Cygnus OB2 No. 12 is due not to a high number density of  $H_3^+$  but simply to a long column length. Our calculation is much cruder than that of van Dishoeck and Black but is essentially the same as far as the  $H_3^+$  chemistry is concerned, except that a revised recombination rate is used.

## 4 H<sub>3</sub> + chemistry

A very attractive aspect of  ${\rm H_3}^+$  as a molecular astronomical probe is its simple chemistry. The simplicity of the chemistry allows us to make relatively simple and reliable arguments about the  ${\rm H_3}^+$  number densities and other astrophysical quantities. In the following, we give a crude order of magnitude discussion of its chemistry; more detailed chemical model calculations such as those given by Lee *et al.*<sup>21</sup> and by van Dishoeck and Black<sup>20</sup> are of course desirable for more accurate discussions.

# 4.1 H<sub>3</sub> + chemistry in dense clouds

In cold dense clouds, which are protected from star radiation,  $H_3^+$  is produced almost exclusively from the cosmic ray (CR) ionization of  $H_2$  to  $H_2^+$ ,

$$H_2 \xrightarrow{CR} H_2^+ + e^- \tag{IV}$$

followed by the ion-neutral reaction (I). Reaction (I) is many orders of magnitude more rapid than reaction (IV) and the production rate is governed by the rate of reaction (IV), i.e.,  $\zeta[H_2]$ . The cosmic ray ionization rate  $\zeta \approx 10^{-17} \text{ s}^{-1}$  and  $H_2$  number density  $[H_2] \approx 10^4 \text{ cm}^{-3}$  yield an  $H_3^+$  production rate of ca.  $10^{-13} \text{ cm}^{-3} \text{ s}^{-1}$ .  $H_3^+$  is destroyed predominantly by the proton hop reaction (II). Equating the pro-

duction and destruction rates, we have the steady-state equation

$$\zeta[H_2] = \sum_{x} k_x [H_3^+][X]$$
 (3)

where  $k_x$  is the rate constant for reaction (II). Since CO is the most abundant molecule in dense clouds, we neglect the terms of the other atoms and molecules in eqn. (3) and obtain the H<sub>3</sub> + number density

$$[\mathrm{H_3}^+] = \frac{\zeta}{k_{\mathrm{CO}}} \frac{[\mathrm{H_2}]}{[\mathrm{CO}]} \tag{4}$$

Since the ratio  $[H_2]/[CO] \approx 10^4$  is approximately constant over a wide variety of molecular parameters, <sup>21</sup> this shows that  $[H_3^+]$  is constant. Using the Langevin rate  $k_{\rm CO} \approx 10^{-9}$  cm<sup>3</sup> s<sup>-1</sup> we obtain  $[H_3^+] \approx 10^{-4}$  cm<sup>-3</sup>. The observed  $H_3^+$  column density of  $3 \times 10^{-14}$  cm<sup>-2</sup> (see Table 1) gives a typical effective column length of  $\approx 1$  pc.

The most serious omission in this discussion is the neglect of X terms other than CO from eqn. (3). In the model calculations of Lee et al., 21 the abundance of O is predicted to be comparable to that of CO. Inclusion of the O term will reduce the  $[H_3^+]$  by ca. 30% since the rate constant  $k_0$  is about 1/2.5 of  $k_{CO}$ .<sup>64</sup> The neglect of the electron term  $X = e^-$  in eqn. (3) also has to be addressed since the recombination rate constant  $k_{\rm e}$  is larger than  $k_{\rm CO}$  by more than two orders of magnitude (see Section 4.2). However, the model calculations of Lee *et al.*<sup>21</sup> show that this correction is significant only in clouds with high metallicity, where the electron concentration is increased by the ionization of alkali and alkaline-earth metals with low work functions. The lack of accurate measurements of  $k_{\rm O}$  (and for that matter even of  $k_{\rm CO}$ ) is also a source of error and more laboratory studies are awaited.

However, all these corrections will be small compared to the large uncertainty in  $\zeta$ . We hope that our H<sub>3</sub><sup>+</sup> measurements will help further constrain this important param-

#### 4.2 H<sub>3</sub> + chemistry in diffuse clouds

In diffuse clouds where the number density is low (10–10<sup>3</sup> cm<sup>-3</sup>) and visible light passes through, cosmic ray ionization followed by reaction (I) is again the primary mechanism for H<sub>3</sub><sup>+</sup> production. Photoionization of H<sub>2</sub> is not effective because the cloud contains abundant atomic H atoms whose ionization potential (13.6 eV) is lower than that of H<sub>2</sub> (15.4 eV).

The main destruction mechanism of H<sub>3</sub><sup>+</sup> in diffuse clouds is expected to be electron recombination, because of the high number density of electrons created by photoionization of carbon (the carbon atom has the lowest ionization potential, 11.3 eV, of any abundant species). We assume for simplicity that all carbon atoms which are not depleted onto dust grains are ionized and that all electrons come from the ionization of carbon atoms, i.e.,  $[e^-] = [C^+] = [\Sigma C]$ , where  $[\Sigma C]$  denotes the total number density of carbon atoms. The solution of the steady state equation is then

$$[\mathbf{H_3}^+] = \frac{\zeta}{k_e} \frac{[\mathbf{H_2}]}{[\mathbf{e}^-]} \tag{5}$$

indicating that the  ${\rm H_3}^+$  number density is constant also in diffuse clouds. Using  $k_{\rm e}\approx 10^{-7}~{\rm cm}^3~{\rm s}^{-1~63}$  and  ${\rm [H_2]/[e^-]}\approx {\rm [H_2]/[\Sigma C]}\approx 10^4$  we obtain an  ${\rm H_3}^+$  number

density of  $[H_3^+] \approx 10^{-6}$  cm<sup>-3</sup>, smaller than that of dense clouds by two orders of magnitude. Thus the same  $H_3^+$  column density as in dense clouds  $(3 \times 10^{14} \text{ cm}^{-2})$  implies an effective path length (L) that is longer by two orders of magnitude,  $L \sim 100$  pc. This path length is very likely composed of several diffuse clouds rather than a single cloud.

There is a major uncertainty in the above estimates, apart from that of  $\zeta$ . Unlike other  $k_x$  with Langevin rates, which are independent of temperature,  $^{65,66}$   $k_e$  varies significantly at low temperature. If we use  $k_e = 4.6 \times 10^{-6}/T^{0.65}$  cm<sup>3</sup> s<sup>-1</sup>, as determined from the storage ring experiment of Sundström *et al.*,  $^{67}$  and assume  $T \approx 30$  K,  $k_e$  is closer to  $10^{-6}$  cm<sup>3</sup> s<sup>-1</sup> and  $L \approx 1$  kpc. In addition, we have not considered direct photodissociation of  $H_3^+$ . This is thought to be slow  $^{68}$  but more theoretical and experimental studies are certainly needed.

#### 4.3 Intermediate case

The above two analyses for the extreme cases can be generalized to the intermediate case where the destruction rates of  $H_3^+$  by CO and by electrons are comparable. We assume that all carbon atoms in the gas phase are either in the form of  $C^+$  or CO, that is,  $[\Sigma C] = [C^+] + [CO]$ , where  $[\Sigma C]$  denotes the total number density of carbon atoms in any gaseous form. Other carbon species (atomic C, CO<sub>2</sub>, CH<sub>4</sub>, etc.) can be included in [CO] since they all have Langevin rates for the proton hop reaction (II). We have

$$[\mathrm{H_3}^+] = \zeta \, \frac{f}{2} \, \frac{[\Sigma \mathrm{H}]}{[\Sigma \mathrm{C}]} \left[ \frac{1}{k_e (1 - \alpha) + k_{\mathrm{CO}} \alpha} \right] \tag{6}$$

where f is the fraction of hydrogen atoms in molecular form  $f \equiv 2[\text{H}_2]/[\Sigma \text{H}]$  and  $\alpha$  is the fraction of carbon atoms in molecular form,  $\alpha \equiv [\text{CO}]/[\Sigma \text{C}]$ . For derivation of this formula and further discussions of the total number density  $[\Sigma \text{H}]$  and path length L of the cloud, see McCall et al.<sup>61</sup>

#### 5 Future prospects

Our observations have established that interstellar  $H_3^+$  exists with sufficient abundance to be observable from ground-based observatories both in dense and diffuse clouds. In fact, we find it easier to observe  $H_3^+$  absorption lines than  $H_2$  infrared absorption lines. Perhaps  $H_3^+$  is not only a powerful probe for the study of plasma activities of astronomical objects, but also a most convenient probe for the detection of hydrogenic molecular species. In the spirit of this conference, we speculate in this section on some possible developments in the immediate future.

#### 5.1 Future observations

From ground-based observatories,  $H_3^+$  will be found in many other sources. For dense clouds the observations will give information of the depth of the embedded YSO and for diffuse clouds they will give the dimension of the clouds. For a source like the Quintuplet near the galactic center where many infrared sources are positioned within a narrow angle of sight, some type of 'mapping' such as radioastronomers do might be possible. This will be most efficiently done when the Phoenix spectrometer is moved to the Cerro Tololo Interamerican Observatory next year (1999). The expected advent of larger telescopes with high-resolution infrared spectrometers, such as Gemini and Subaru, and the installation of a high-resolution spectrometer at Keck will allow us to observe much fainter infrared sources.  $H_3^+$  will be observed in a great many more

objects with higher spectral resolution. We may not have to wait many years before  $H_3^+$  is observed in extragalactic objects.

## 5.2 H<sub>3</sub> + emission

Observing the infrared spectrum of  ${\rm H_3}^+$  in emission is an interesting possibility. One remembers the strong and pure  ${\rm H_3}^+$  emission lines observed in planetary ionospheres. The strongest  ${\rm H_2}$  quadrupole emission line  ${\rm S_1}(1)$  (with a spontaneous emission lifetime of  $7\times 10^6$  s  $^{69}$ ) is observed with large signal to noise ratios in planetary nebulae,  $^{70}$  extragalactic superluminous objects,  $^{71}$  and many other objects, even using low resolution spectrometers. In order to evaluate the prospects for detecting  ${\rm H_3}^+$  emission we make a rough estimate of the ratio of intensities for  ${\rm H_3}^+$  emission,  $I_{{\rm H_3}^+}$ , and  ${\rm H_2}$  emission,  $I_{{\rm H_2}}$ :

$$\frac{I_{\rm H_3^+}}{I_{\rm H_2}} = \frac{[\rm H_3^+]}{[\rm H_2]} \frac{k_{\rm H_3^+}}{k_{\rm H_2}} \tag{7}$$

where  $k_{\rm H_3^+}$  and  $k_{\rm H_2}$  are rate constants for collisional pumping from v=0 to v=1. We estimate that the abundance of  ${\rm H_3^+}$  should be roughly  $[{\rm H_3^+}]/[{\rm H_2}] \approx 10^{-8}$ , which one would think would make the ratio small. However, we must consider the differences in the vibrational pumping mechanisms. The collisional excitation of  ${\rm H_2}$  by  ${\rm H_2}$ 

$$H_2 + H_2 \to H_2^* + H_2$$
 (V)

is performed by a weak physical interaction, in which the translational energy of  $H_2$  must be converted to vibrational energy (V-T transfer) during the short time of the encounter. Resonant V-V transfer cannot contribute, since the number of  $H_2^*$  remains the same in the 'reaction'  $H_2^* + H_2 \rightarrow H_2 + H_2^*$ .

On the other hand, the excitation of  $H_3^+$  is performed by a strong chemical interaction

$$H_3^+ + H_2 \rightarrow H_3^{+*} + H_2$$
 (VI)

where asterisks signify vibrational excitation. In this case, the molecules attract each other by the Langevin force, form an activated complex  $({\rm H_5}^+)^*$ , and then dissociate into  ${\rm H_3}^+*$  and  ${\rm H_2}$ . This reaction is known to have a Langevin rate from a deuterium experiment and a recent experiment of spin modification. The branching ratio of reaction (VI) to form  ${\rm H_3}^+$  or  ${\rm H_3}^+*$  is not known but we assume that it is not much different from 1:1. Then using the approximate equality between the Langevin rate and the rate of rotational energy transfer (R-R), and the rule of thumb  ${}^{74}k_{\rm V-T}/k_{\rm R-R}\approx 10^{-5}$ , we obtain  $k_{\rm H_3}+/k_{\rm H_2}\approx 10^5$ . If we use experimental and theoretical  $v'=1\to 0$  deexcitation rates and the principle of detailed balancing, we find that  $k_{\rm H_3}+/k_{\rm H_2}\approx 10^5-10^6$  for T=2000-1000 K.

Thus we obtain an estimate of  $I_{\rm H_3^+}/I_{\rm H_2} \approx 10^{-3} - 10^{-2}$ . This is a minimum value and will be larger for a molecular cloud with a density higher than the critical density.<sup>76</sup> In such a high-density environment, the  ${\rm H_3}^+$  intensity will be increased due to the faster collisional pumping (as  ${\rm H_3}^+$  has a spontaneous emission time of only  $\approx 10~{\rm ms}^{77}$ ), but the  ${\rm H_2}$  intensity will be limited by the slower rate of spontaneous emission.

Even if  $I_{\rm H_3}{}^+/I_{\rm H_2} \approx 10^{-3}$ , the detection of  $\rm H_3{}^+$  emission is a realistic prospect in view of the extremely high observed signal to noise ratios of  $\rm H_2{}$  emission ( $\gtrsim 1000$  at low resolution).

## 5.3 H<sub>3</sub> + as an interstellar agent

Interstellar H<sub>3</sub><sup>+</sup> not only plays the central role of the protonator to initiate a network of chain reactions, but also performs other essential functions of interstellar chemistry. For

example, it will mediate conversion of ortho-H<sub>2</sub> to para-H<sub>2</sub> through the proton hop reaction

$$H_3^+ + \tilde{H}_2 \to H_2 + \tilde{H}_2 H^+$$
 (VII)

and proton exchange reaction

$$H_3^+ + \tilde{H}_2 \rightarrow H_2 \tilde{H}^+ + H \tilde{H}$$
 (VIII)

This scrambling of protons will thermalize spin modifications. The actual efficiency of this mechanism should be calculated using the nuclear modification branching ratios theoretically predicted by Quack<sup>78</sup> and recently experimentally demonstrated.<sup>72</sup> These processes must be much more efficient than the mechanism proposed earlier<sup>79</sup>

$$H^+ + o - H_2 \rightarrow H^+ + p - H_2$$
 (IX)

both because of the higher abundance of  $H_3^+$  and the higher rate constant of reactions (VII) and (VIII) than (IX).

Klemperer and Miller<sup>80</sup> have recently proposed that the strong CO Cameron band emission (a  ${}^3\Pi \to X\, {}^1\Sigma^+$ ) from 1850–2600 Å observed in the Red Rectangle nebula<sup>81,82</sup> might be due to a chemical pumping of CO by  $H_3^+$  through the reactions

$$H_3^+ + CO \rightarrow HCO^+ + H_2 \tag{X}$$

and

$$HCO^+ + e^- \rightarrow CO^* + H$$
 (XI)

where the asterisk signifies CO in the a  $^3\Pi$  excited state. In diffuse clouds where  $[e^-] \gg [CO]$ , the second reaction is much faster than the first and the rate for CO\* excitation is  $k_{\rm CO}[{\rm H_3}^+][{\rm CO}] \approx 10^{-26}~{\rm cm}^{-3}~{\rm s}^{-1}$  (here again we neglect the branching ratio between CO and CO\*). Glinski *et al.*<sup>81</sup> proposes the direct electron pumping

$$CO + e^{-*} \rightarrow CO^* + e^{-}$$
 (XII)

to be the main mechanism where  $e^{-*}$  signifies electrons at high energy  $\approx 8-12$  eV. The rate of this process is  $k[CO][e^{-*}]$  where the rate constant of excitation k is  $\approx 10^{-8}$  cm<sup>3</sup> s<sup>-1</sup>. Thus the relative efficiency of the  $H_3^+$  pumping of Klemperer and Miller and the electron pumping of Glinski *et al.* depends on the relative magnitudes of  $[H_3^+]$  and  $10[e^{-*}]$ . It is quite probable that  $H_3^+$  is the agent for the emission, especially for the rotationally cold emission core.

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